

# **THE STUDY OF CO<sub>2</sub> TRANSCRITICAL CYCLE WATER SOURCE HEAT PUMP AND THE ANALYSIS OF THE APPLICATION**

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## **ABSTRACT**

The characteristics of CO<sub>2</sub> transcritical cycle heat pump such as the optimum high pressure, the maximum COP, the influence of evaporating temperature and outlet refrigerant temperature of gas cooler are analyzed in this paper. More over, through the analysis of expanding process, the ideal CO<sub>2</sub> expander demands are provided and the design technical direction of CO<sub>2</sub> is also pointed out. In addition, CO<sub>2</sub> transcritical cycle water source heat pump for hot water space heating is studied theoretically. By the comparison with the coal combustion boiler for space heating, we find that the first energy utilization rate of CO<sub>2</sub> transcritical cycle water source heat pump is higher. Furthermore, the combination of radiant ceiling panels and CO<sub>2</sub> transcritical cycle heat pump is analyzed and conclude that it is a nice and feasible two-win method in techniques. And by calculation and comparison, we obtain that CO<sub>2</sub> transcritical cycle with both expander and internal heat exchanger is the most suitable cycle to incorporate with the radiant ceiling panels if it is applied for both heating in winter and cooling in summer.

## **1. INTRODUCTION**

Water source heat pump can not only meet the need of clean heating, but also has some advantages such as high energy efficiency, not being influenced by the air temperature of different seasons, no frost infection and effective application of waste heat. Therefore, it got fully developed from the middle of the 20<sup>th</sup> century.

However, the conventional refrigerants such as Chlorofluorocarbons (CFCs) and Hydro chlorofluorocarbons (HCFCs) are now being regulated because of ozone depletion and global warming. Replacing (H)CFCs by HFCs and HFC mixtures still means using fluids with a large global warming potential. Simple logic indicates that substances present naturally in the biosphere, and for which the effects are long established, must be generally preferred as refrigerants (Lorentzen and Pettersen 1993). Carbon dioxide is one of these nature refrigerants.

Carbon dioxide was a commonly used refrigerant from the late 1800s and well into the 20<sup>th</sup>

century. Owing to its complete harmlessness it was the generally preferred choice for usage on board ships. With the advent of the freones, the use of CO<sub>2</sub> was rapidly interrupted for the rapid loss of capacity at high cooling-water temperatures in tropics and the failure of the manufacturers to follow modern trends in CO<sub>2</sub> design towards more compact and price-effective high-speed types. The time is now ripe for application with present-day technology (Lorentzen 1994).

Carbon dioxide has many advantages as refrigerant in transcritical cycle such as Environmentally benign (ODP=0, GWP=1), safe (non-toxic & non-flammable), low cost, high volumetric capacity (compact systems), high thermal conductivity, low dynamic viscosity, compatible with normal lubricants and construction materials, low pressure ratio, low service cost (no reclamation), and considerable experience available. In addition, the heat rejection is in supercritical area, so the CO<sub>2</sub> discharge temperature of the compressor is high (can up to 100°C) and the gliding temperature is also high. Generally using conventional work medium the temperature of supplied hot water can only exceed to 50-55°C at present. If raising the hot water temperature the condensing pressure would be too high, which will lead to the poor performance of the system. CO<sub>2</sub> transcritical cycle water source heat pump system, however, can rise the temperature of geothermal water, industrial waste water and the 30-60°C underground water through the first heat pump temperature rising to more than 80°C in order to supply space heat and other usages such as dehumidification. With the rapid increase of the city-heating load and the air-conditioned space, the system can partly replace the coal to supply heat so as to alleviate the city environment pollution and reduce the CO<sub>2</sub> emission.

**2. THE CHARACTERISTICS OF CO<sub>2</sub> TRANSCRITICAL CYCLE HEAT PUMP**

**2.1 The optimum high pressure and the maximum COP**

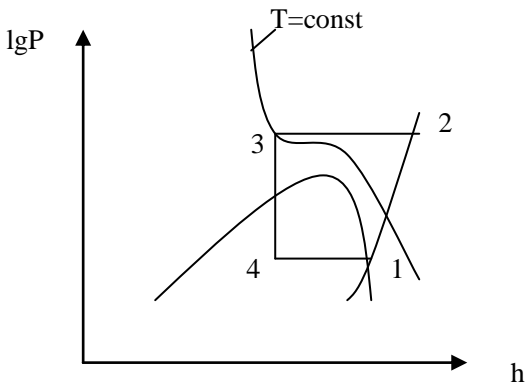


Figure1 LgP-h diagram for the transcritical cycle

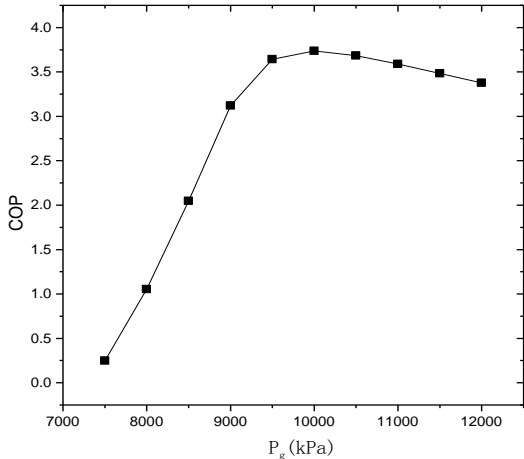


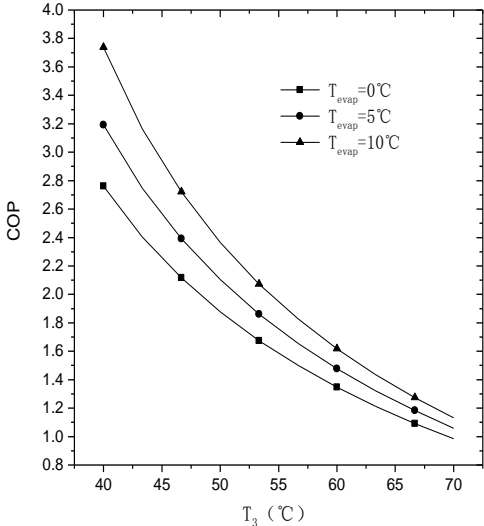
Figure2 Influence of P<sub>g</sub> on COP

As shown in Figure1, the heat absorption and the heat rejection process of CO<sub>2</sub> are in two-phase and supercritical areas respectively. In conventional subcritical cycles, the enthalpy of the condenser outlet liquid is only the function of temperature. While in the supercritical area of

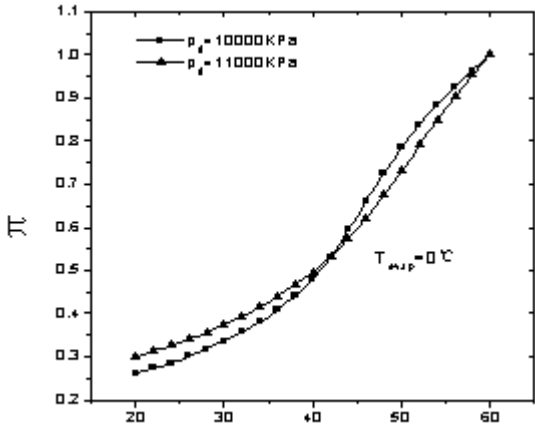
the transcritical cycle, the pressure and the temperature are two independent variables, which determine the fluid enthalpy at the same time. It is illustrated clearly from the S-shape isothermal line in the supercritical area in Figure 1. Assuming a constant evaporating temperature  $T_4$  and a constant refrigerant temperature at the gas cooler outlet  $T_3$ , variation of the high pressure  $P_3$  leads to a change in refrigeration capacity, the shaft power and the coefficient of performance COP. The COP has a maximum value depending on  $P_3$ , because of the S-shape of the isotherm line and the straight compression line (Kauf 1999). With the rising of  $P_3$ , the isothermal line becomes steep, which demonstrates that the increase speed of the refrigeration capacity reduces with the enhancement of the pressure. But the isotropic line is almost a straight line, so the shaft power increases nearly linearly with the enhancement of the pressure.

Figure 2 shows the theoretically calculated COP at different pressure  $P_g$  when  $T_4=10^\circ\text{C}$  and  $T_3=40^\circ\text{C}$ . At the beginning COP increases quickly, and then increases gently, at last it becomes decreasing. When the pressure is about 10 Mpa, the system got the maximum COP.

**2.2 The influence of  $T_{\text{evap}}$  and  $T_3$  on the performance of the cycle**



**Figure 3** COP at different  $T_3$  and different  $T_{\text{evap}}$



**Figure 4** The loss ratio at different  $T_3$

Figure 3 illustrates the COP at different  $T_3$  and different evaporating temperature  $T_{\text{evap}}$ . COP decreases with the dropping of  $T_{\text{evap}}$  and decreases very quickly with the rising of  $T_3$ . The primary reason is the throttling loss increases sharply with the rising of  $T_3$ . Figure 4 demonstrates that the throttling losses of  $\text{CO}_2$  transcritical cycle at different  $T_3$  when the evaporation temperature is  $0^\circ\text{C}$ .  $\pi$  refers to the loss ratio of the throttling loss when the refrigerant temperature before throttling is  $T_3$  to the throttling loss when that is  $60^\circ\text{C}$ . The throttling valve loss occupies the largest part in all the losses of the cycle (Ma et al. 2001).

Using expander to replace the throttling valve is a very effective way to decrease the loss and improve the COP of the cycle (Ma 1999). The cycle with expander is approach to the ideal Carnot cycle, and there is no throttling loss theoretically. So the COP is higher than the conventional cycle. Moreover, the expanding ratio of  $\text{CO}_2$  transcritical cycle is small (only 2-4), and the expanding power is large (25%-30% of the compressor shaft power). Therefore, the replacement is applicable from both theoretical and technical points of view.

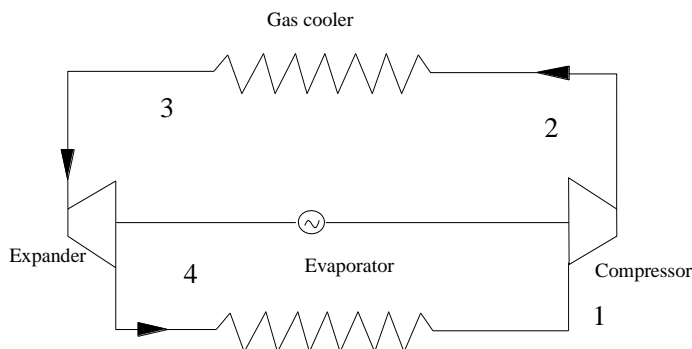
**2.3 Large gliding temperature in the heat rejection process**

The large gliding temperature in the heat rejection process can match well with the heat media, and satisfy the stage application of the heat pump.

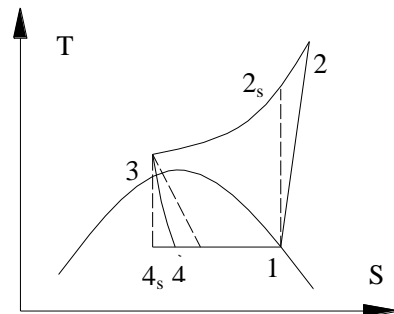
### 3. THE ISSUES IN THE EXPANDER DESIGN

In the CO<sub>2</sub> transcritical cycle, the inlet refrigerant of the expander is in the supercritical area. So the density resembles to the liquids and it has good mobility. First, the supercritical fluid changes to the high-pressure liquid. Then there are boiling cores form, which produce bubbles in the high-pressure liquid. The bubbles grow up and expand to output mechanical power. According to the process, the ideal expander should meet the demands as follows:

- a. High pressure (up to 15Mpa) resistant
- b. Can work in gas-liquid two phase area and stand for both liquid-slugging and gas-erosion
- c. Small volume
- d. Hermetically sealed
- e. High entropy efficiency more than 60%
- f. Work stably and available for high velocity
- g. Enough intensity



**Figure 5a** Diagram of CO<sub>2</sub> transcritical cycle with expander



**Figure 5b** T-S Diagram of CO<sub>2</sub> transcritical cycle with expander

To improve the hermetical performance of the expander in the high pressure we plan to design the expander and the compressor at the same shaft as shown in Figure 5a. Another advantage of this kind of design is that the compressor can use the recovery power effectively. If the mechanical construction can achieve technically, it is even better to incorporate the expander and the compressor into one shell to become a semi-hermetical or hermetical expander-compressor.

## 4. CO<sub>2</sub> TRANSCRITICAL CYCLE WATER SOURCE HEAT PUMP APPLICATIONS

### 4.1 CO<sub>2</sub> transcritical cycle water source heat pump for hot water space heating

In the calculation of the CO<sub>2</sub> transcritical cycle water source heat pump applying to hot water space heating, we assume that the outlet refrigerant of the evaporator is saturated vapor; the isentropic efficiency of the expander is 65%; the isentropic efficiency of the compressor is

80%; other irreversible loss can be neglected; the temperature difference between  $T_3$  and return water temperature is  $5^\circ\text{C}$ ; the COP and high pressure of the system is the optimum value at the operation condition. When the supply water and return water temperature are  $95^\circ\text{C}$  and  $55^\circ\text{C}$  respectively (standard high temperature heating supply) and when  $T_3$  is  $60^\circ\text{C}$ , the calculation results are shown in Figure 6 and Figure 7.

From the viewpoint of the first energy utilization rate, we can compare the heating supply methods of coal combustion boiler and the heat pump (Hong 2000).

The first energy utilization rate of coal combustion boiler heating can be calculated as:

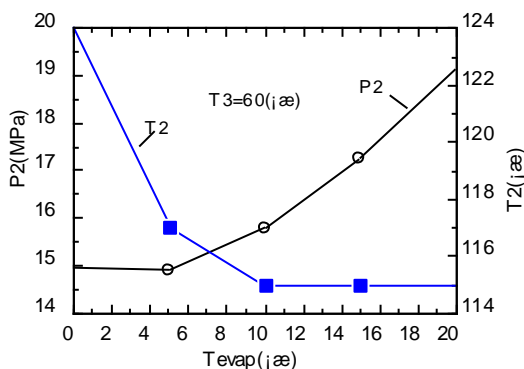
$$m_b = \frac{1000 \times 3600}{H \cdot \eta} = \frac{1000 \times 3600}{29260 \times 0.6} = 205 \text{ kg} / 1000 \text{ kW} \cdot \text{h} \quad (1)$$

The average efficiency of coal combustion boilers for heating in China is  $\eta = 55\% - 60\%$ . In this calculation, we assume  $\eta = 60\%$ .  $H$  is the thermal capacity of standard coal, we assume  $H = 29260 \text{ kJ/kg}$ .

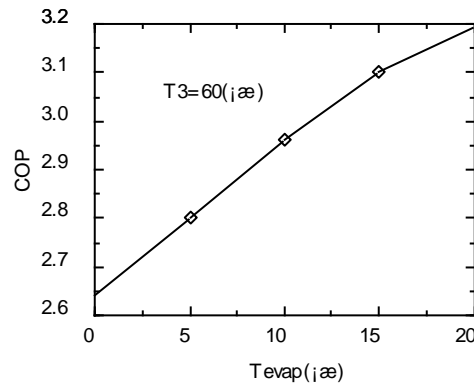
The first energy utilization rate of heat pump heating can be calculated as:

$$m_{hp} = \frac{1000 \times b}{COP} = \frac{1000 \times 0.4}{2.0} = 200 \text{ kg} / 1000 \text{ kW} \cdot \text{h} \quad (2)$$

$b = 0.4 \text{ kg} / \text{kW} \cdot \text{h}$ , which is the standard coal consumption of power plants at present. By the comparison, we conclude that the first energy utilization rate of the heat pump is smaller than that of the coal combustion boiler for heating supply unless the COP is larger than 2. Figure 7 shows that the COP is larger than 2 at evaporating temperature range of 5 to  $20^\circ\text{C}$ . Therefore, the  $\text{CO}_2$  transcritical cycle water source heat pump is better than the coal combustion boiler for hot water space heating at the aspect of first energy utilization rate.



**Figure 6** Inlet refrigerant pressure and temperature of the gas cooler at different evaporating temperature

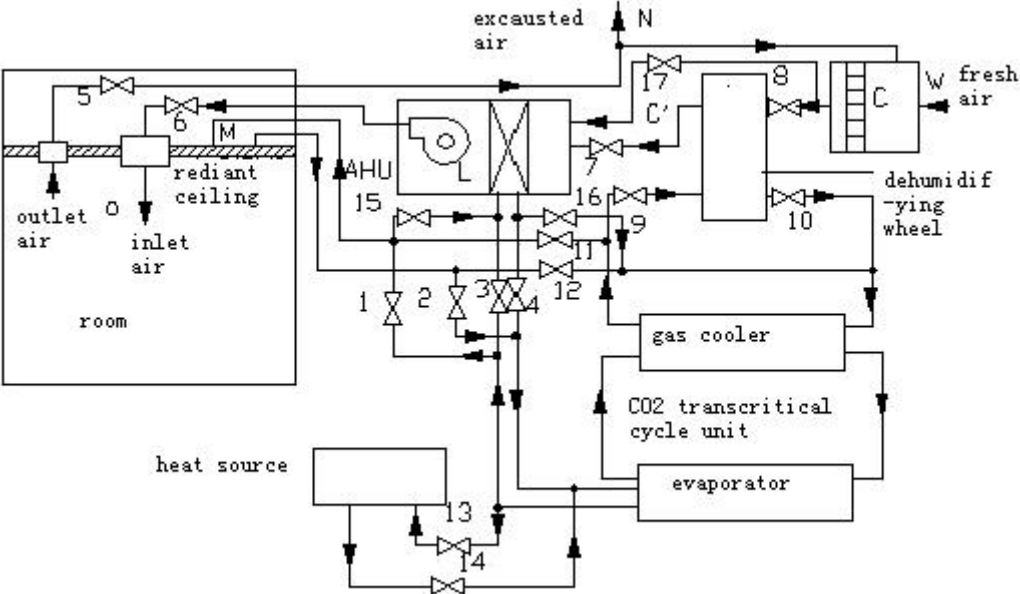


**Figure 7** COP of the system at different evaporating temperature

#### 4.2 A combination of radiant ceiling panels and $\text{CO}_2$ transcritical cycle in air conditioning system

From the analysis above, we admit that  $\text{CO}_2$  transcritical cycle has advantages in space heating. However, it also has the disadvantage of low COP in air-conditioning in summer because of the great quantity of discharge heat of the gas cooler. The combination of radiant ceiling panels and  $\text{CO}_2$  transcritical cycle heat pump is a nice and feasible two-win method in

techniques. Applying radiant technology in Air conditioning systems of buildings has some comprehensive advantages in several aspects such as comfort, energy conservation and space saving. However, we have to solve the problem of humidity to avoid condensation of the panels, if we apply the radiant ceiling panels in the air conditioning system in humid climate. Using CO<sub>2</sub> as refrigerant in the transcritical cycle heat pump also possesses the merits in environment (ODP=0, GWP=1), but its efficiency is relatively low. A good improving way is to recover the discharge heat. Utilizing the heat of discharge gas as heat source of desiccant equipment can not only save the cost of the heating power, but also can improve the energy utilization rate of the CO<sub>2</sub> transcritical cycle heat pump (Zha et al. 2001). Moreover, the temperature of the water flowing in radiant ceiling panels is relatively high, so the evaporating temperature of the CO<sub>2</sub> transcritical cycle heat pump can be increased. Therefore, the COP of the system can also increase. In addition, the radiant ceiling panels can incorporate with the room fitment and decoration so that the radiant ceiling panels can not only be used as the room ceil, but also supply heating in winter and cooling in summer. The combination system is also adaptable to the place where has restrict on noise, vibration and stability of the room temperature. The schematic picture of the system is provided as Figure 8.



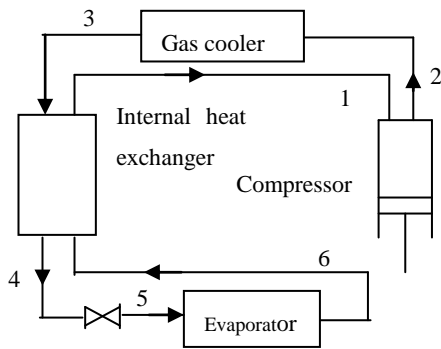
**Figure 8** The schematic picture of the combination system of radiant ceiling panels and CO<sub>2</sub> transcritical cycle heat pump

The system consists of CO<sub>2</sub> transcritical cycle heat pump unit, dehumidifying unit, air mixing unit, air handling unit(AHU) and radiant ceiling panels unit. The system can supply both heating and cooling in a year. In summer, the valve 1-10 open, 11-17 close. Due to the high humidity in summer, the mixture of the fresh air and the return air enter the dehumidifying wheel, then pass through the heat exchanger to lower the temperature and to be dehumidified before entering the air-conditioned room. The heat exchanger is cooled by the evaporator of the CO<sub>2</sub> transcritical cycle heat pump and the dehumidifying wheel is heated by the gas cooler of the CO<sub>2</sub> transcritical cycle heat pump. The radiant ceiling panels is also cooled by the evaporator of the CO<sub>2</sub> transcritical cycle heat pump.

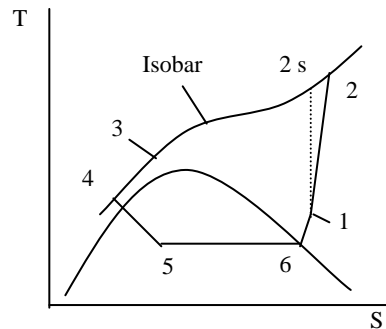
In winter, the valve 11-17open, 1-10 close. The dehumidify unit stops working. The radiant

ceiling panels and air-handling unit are both heated by the gas cooler of the CO<sub>2</sub> transcritical cycle heat pump. The operation will need low temperature heat source such as ground water and the surface water in warm area.

For the calculation of the CO<sub>2</sub> transcritical cycle water source heat pump, we assume that the outlet refrigerant of the evaporator is saturated vapor; the isentropic efficiency of the expander is 65%; the isentropic efficiency of the compressor is 80%; the superheat of the internal heat exchanger is 15°C; Other irreversible loss can be neglected. We can compare (a) the CO<sub>2</sub> transcritical cycle with internal heat exchanger (Figure 9), (b) CO<sub>2</sub> transcritical cycle with expander (Figure 5) and (c) CO<sub>2</sub> transcritical cycle with both expander and internal heat exchanger. To save energy and to avoid dew condensing on the radiant ceiling panels, we let the evaporating temperature 10°C. When T<sub>3</sub> is 40°C, the calculation results are shown in Table 1.



**Figure 9a** Diagram of CO<sub>2</sub> transcritical cycle with internal heat exchanger



**Figure 9b** T-S diagram of CO<sub>2</sub> transcritical cycle with internal heat exchanger

**Table 1. The calculation results of the (a)(b)(c) three kinds of cycles**

	P <sub>2</sub> (MPa)	T <sub>2</sub> (°C)	COP <sub>h</sub>	COP <sub>r</sub>	P <sub>2</sub> (MPa)	T <sub>2</sub> (°C)	COP <sub>h</sub>	COP <sub>r</sub>	P <sub>2</sub> (MPa)	T <sub>2</sub> (°C)	COP <sub>h</sub>	COP <sub>r</sub>
<b>a</b>	8	74.1	2.6	1.6	10	94.7	4.1	3.1	11	103.8	3.9	2.9
<b>b</b>	9.5	74.4	5.0	4.0	12.5	93.9	4.4	3.4	13.5	100.7	4.2	3.2
<b>c</b>	8	74.1	3.6	3.5	10	94.7	4.8	4.4	11	103.8	4.5	4.0

P<sub>2</sub>, T<sub>2</sub>: The pressure and temperature of the inlet refrigerant of the gas cooler

COP<sub>h</sub>, COP<sub>r</sub>: the heating COP and cooling COP of the cycles

It is demonstrated that cycle b has the highest COP when T<sub>2</sub> is less than 80°C. When it is used for heating by radiant ceiling panels only in winter, cycle b is the most suitable one. However, when it is used for cooling by radiant ceiling panels in summer, b is not suitable. Because dehumidify unit must be working in humid area such as Southeast China in summer. Generally the inlet temperature of regeneration air of air-conditioning dehumidifier must be higher than 80°C. T<sub>2</sub> should be higher than 90°C since the discharge heat of the gas cooler is used to heat the regeneration air. Both cycle a and c can meet the need. But cycle c has the highest COP when T<sub>2</sub> is higher than 94°C and it is more close to the optimum pressure. Therefore, cycle c is the most suitable one if it is used to both heating in winter and cooling in

summer.

When  $T_2$  is  $103.8^\circ\text{C}$ ,  $\text{COP}_h$  of cycle c can exceed to 4.5 and  $\text{COP}_r$  can exceed to 4.0. The dehumidify cooling COP based on the heat capacity for the regeneration air is 0.5 (Wang et al. 2000). If the dehumidifying unit is taken into consideration, the combination efficiency can be calculated as:

$$\text{In summer: } \text{COP}_r=4.0+0.5(1+4.0)=6.5 \quad (3)$$

$$\text{In winter : } \text{COP}_h=4.5$$

Both of them are higher than the efficiency of the conventional refrigerant cycle.

The radiant heat capacity can be calculated as:

$$Q_r = F_{12}A_{eff}\varepsilon_1\varepsilon_2\sigma(T_1^4 - T_2^4) \quad (4)$$

Where,  $T_2 = (T_i + T_o)/2$

$F_{12}$ : View factor

$\varepsilon_1$ : Emissivity of surrounding surface

$\varepsilon_2$ : Emissivity of radiator surface

$\sigma$ : Stefan-Boltzman constant [ $5.57 \times 10^{-8} \text{ W}/(\text{m}^2 \cdot \text{K}^4)$ ]

$T_1$ : Average temperature of surrounding surfaces [K]

$T_2$ : Mean radiator surface temperature [K]

$T_i$ : Water inlet temperature [K]

$T_o$ : Water outlet temperature [K]

In winter, the radiant ceiling removes the heat load of the room, while air handling unit (AHU) removed the fresh air load. The heat load distribution of the gas cooler can be regulated according to the fresh air rate. In summer, the radiant ceiling removes the sensible load of the room, the dehumidify wheel removes the latent load and AHU removes both part of sensible load and part of latent load.

## 5. DISCUSSION

Although the calculated COP of the  $\text{CO}_2$  transcritical cycle heat pump applied to hot water space heating is higher than 2.6, the practical COP may be lower than the calculated one. Because in the calculation we assume that the outlet refrigerant of the evaporator is saturated vapor; the isentropic efficiency of the expander is 65%; the isentropic efficiency of the compressor is 80%; other irreversible loss can be neglected. However, there still exist room to improve the energy application efficiency. As it is shown in Figure 3 that with the rising of  $T_3$ , the COP decreases very quickly. In the calculation,  $T_3$  is set to  $60^\circ\text{C}$  to match the standard high temperature heating supply ( $95^\circ\text{C}/55^\circ\text{C}$ ). If we apply the stage energy, for instance, using the  $55^\circ\text{C}$  return water to supply heat though radiant floor, the energy efficiency can be greatly improved.

By the calculation, we find cycle c is the most suitable cycle to the combination air conditioning system of radiant ceiling panels and  $\text{CO}_2$  transcritical cycle. However, the initial cost of the system have to increase because the system not only affiliates an internal heat exchanger, but also applies a  $\text{CO}_2$  expander though the efficiency of cycle c can be improved

greatly because of the improved evaporating temperature and the recovered power of the expander. The price of internal heat exchanger is not high and some conventional cycle also often affiliates it to improve the efficiency. Therefore, the technical development and the cost reduction of the expander are crucial to the popular application of the system. We suppose that combining the function of the CO<sub>2</sub> compressor and the CO<sub>2</sub> expander in one part is the developing direction because the seal and the power recovery can be achieved easily.

The area control can also be achieved easily due to the adoption of radiant ceiling panels. But the thermal capacity of the radiant ceiling panels is relatively large, so the parameters control may be lagged behind. Further research is needed in the system matching and system control.

## 6. CONCLUSION

Because the CO<sub>2</sub> transcritical cycle is in the supercritical area, the pressure and the temperature are two independent variables, which determine the fluid enthalpy at the same time. And there exists an optimum high pressure and the maximum COP due to the S-shape isothermal line in the supercritical area.

- COP decreases with the dropping of  $T_{\text{evap}}$  and the COP decreases very quickly with the rising of  $T_3$ . The primary reason is the throttling loss increases sharply with the rising of  $T_3$ . And using expander to replace the throttling valve is a very effective way to decrease the loss and improve the COP of the cycle.
- The large gliding temperature in the heat rejection process of the CO<sub>2</sub> transcritical cycle heat pump can match well with the heat media, and satisfy the stage application of the heat pump.
- To improve the hermetical performance of the expander in the high pressure and to use the recovery power effectively, the expander and the compressor can be designed at the same shaft. If the mechanical construction can achieve technically, it is even better to incorporate the expander and the compressor into one shell to become a semi-hermetical or hermetical expander-compressor.
- The CO<sub>2</sub> transcritical cycle water source heat pump is better than the coal combustion boiler for hot water space heating at the aspect of first energy utilization rate.
- The combination of radiant ceiling panels and CO<sub>2</sub> transcritical cycle heat pump is a nice and feasible two-win method in techniques. And CO<sub>2</sub> transcritical cycle with both expander and internal heat exchanger is the most suitable one if it is used to both heating in winter and cooling in summer.

## ACKNOWLEDGEMENTS

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## REFERENCES

- Hong F., 2000. Theoretical and experimental study on CO<sub>2</sub> transcritical cycle for water-to-water heat pump system, M.S. thesis of Tianjin University.
- Kauf F., 1999. Determination of the optimum high pressure for transcritical CO<sub>2</sub>-refrigeration

cycles, *International Journal of Thermal Science*, Vol. 38, pp. 325-330.

Lorentzen G. and Pettersen J., 1993. A new efficient and environmentally benign system for car air conditioning, *International Journal of Refrigeration*, Vol. 16, No. 1, pp. 4-12.

Lorentzen G., 1994. Revival of carbon dioxide as refrigerant, *International Journal of Refrigeration*, Vol. 17, No. 5, pp. 292-301.

Ma Y.T., Wang K.H., Yang Z. and Lu C.R., 1999. Thermodynamic analysis on CO<sub>2</sub> transcritical cycle with expander, *Journal of Engineering Thermophysics*, Vol. 20, No. 6, pp.662-665.

Ma Y.T., Wei D., Wang J.G., Zha S.T. and Lu C.R., 2001. A Theoretical analysis of the application of the two-phase flow screw expander in CO<sub>2</sub> transcritical refrigeration cycle, *Journal of Engineering Thermophysics*, Vol. 22, No. 2, pp. 137-140.

Wang J.G., Ma Y.T., and Wang K.H., 2000. A combination of CO<sub>2</sub> transcritical cycle and desiccant cooling, *Chinese thermophysical academic conference in thermodynamics and energy application*, pp. 473-477.

Zha S.T., Ma Y.T. and Wang J.G., 2001. A combination of radiant ceiling panels and CO<sub>2</sub> transcritical cycle, *New Technical Development in Refrigeration and Air Conditioner*, pp. 301-306, Shanghai Jiaotong University Press, Shanghai.