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## Numerical investigation on PCM-to-refrigerant heat exchangers for thermal energy storage

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### Abstract

Recently, the application of thermal energy storage systems using phase change materials (PCM) is expanding in many fields due to the high energy storage density of PCMs and the narrow phase-change temperature range. In this paper, we conducted a numerical investigation on a shell-and-tube configured PCM-to-refrigerant heat exchanger (PCMHX) coupled in a vapor compression cycle for personal cooling. The enthalpy method was applied to the phase change analysis. The finite-volume method was employed to address the two-dimensional PCMHX numerical solution. Different from most of the previous studies on PCM-to-water heat exchangers, the proposed PCMHX works as a condenser. We validated the simulation results against the experiment data, including condenser pressure, capacity, and PCM temperature profiles. Since the refrigerant-side heat transfer coefficient changes along the condenser length, the heat transfer flux is not uniform across the PCM. Therefore, we analyzed the uneven PCM melting and its effects on the condensing temperature. Results show that PCM near the condenser outlet melts slower than other sections because of the low heat transfer coefficient and small temperature difference in a subcooled liquid region. The developed PCMHX model can reasonably predict the time-dependent heat transfer performance and the PCM melting process.

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*Keywords:* Modeling; Phase change; PCM-to-refrigerant heat exchanger; Thermal energy storage; Enthalpy method

Nomenclature			
$A, A'$	heat transfer area (mm <sup>2</sup> )	cond	condenser
$C$	specific heat (kJ·kg <sup>-1</sup> ·K <sup>-1</sup> )	dia	diaphragm of TXV
$C_v$	flow coefficient (–)	evap	evaporator
$h$	enthalpy (kJ·kg <sup>-1</sup> )	fin	fin
$H$	latent heat (kJ·kg <sup>-1</sup> )	i	inner
$i, j$	segment number	in	inlet
$k$	thermal conductivity (W·m <sup>-1</sup> ·K <sup>-1</sup> )	ini	initial
$K$	spring constant (N·m <sup>-1</sup> )	isen	isentropic
$L$	length of the PCM cylinder (mm)	l	liquid phase
$Le$	Lewis number (–)	m	melting, motor
$m$	mass (kg)	o	outer
$\dot{m}$	mass flow rate (g·s <sup>-1</sup> )	out	outlet
$N$	rotational speed (rpm)	p	PCM
$P$	pressure (kPa)	r	radial direction
$r, R$	radius (mm)	ref	refrigerant
$t$	time (s)	s	solid phase

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$T$	temperature ( $^{\circ}\text{C}$ )	t	tube
$W$	power consumption (W)	top	top
$y$	deflection of spring in TXV (m)	th	throttle of TXV
$z$	length in z direction (mm)	vol	volumetric
		w	wall
<i>Greek symbols</i>		z	axial direction
$\alpha$	heat transfer coefficient ( $\text{W}\cdot\text{m}^{-2}\cdot\text{K}^{-1}$ )		
$\eta$	efficiency	Abbreviations	
$\rho$	density ( $\text{kg}\cdot\text{m}^{-3}$ )	CENG	compressed expanded natural graphite
$\lambda$	liquid fraction (--)	COP	coefficient of performance
$\delta$	thickness of wall (mm)	MCHX	micro-channel heat exchanger
$\omega$	humidity ratio ( $\text{kg}\cdot\text{kg}^{-1}$ )	MFM	mass flow meter
		PCM	phase change material
<i>Subscripts</i>		PCMHX	PCM heat exchanger
A	ambient	TXV	thermostatic expansion valve
b	bulb sensor of TXV	VCC	vapor compression cycle
comp	compressor		

## 1. Introduction

Phase change material (PCM) coupled heat exchangers are attracting more attention recently since PCM can absorb or release heat within a narrow temperature range. Most PCMHX (PCM heat exchangers) models were developed by commercial CFD software and only a few through self-developed programming [1]. The two most common numerical methods can be used to build the PCM numerical heat transfer model: (1) enthalpy method, (2) effective heat capacity method [1,2]. In the enthalpy method, by introducing enthalpy, the phase change process can be much more straightforward. Latent heat and sensible heat are combined as the enthalpy in the energy equation to avoid nonlinearity in the heat conduction problem [3]. The governing equation is the same for the liquid phase, mushy phase, and solid phase. The melting interface conditions are automatically achieved by evaluating the PCM enthalpy [2,4]. Most PCMs are not pure, and thus phase change occurs over a range of temperatures rather than at a constant temperature. In this paper, a vapor compression cycle (VCC) coupled with PCM through PCMHX was proposed and modeled. The proposed system could be used as a personal cooling system [5,6], in which PCMHX worked as a condenser to store the waste heat to avoid dumping heat to the ambient and reducing human comfort. The enthalpy method was applied to develop the transient model of the refrigerant-to-PCM heat exchanger. We validated the transient VCC system model and PCMHX model against the experimental results, and PCMHX heat transfer characteristics and system performance were also analyzed and discussed in this study.

## 2. System description

The PCM coupled VCC system can be used as a personal cooling system. Using the personal cooling system, the thermal state setting of the building can be higher to reduce the building energy consumption, and meanwhile, occupants can feel comfortable with the localized cooling. The schematic diagram of VCC coupled with PCM through PCMHX is illustrated in Fig. 1(a), in which PCMHX works as a condenser in the VCC system to store the waste heat from refrigerant condensation. So that the heat is not to the ambient and cannot reduce the human comfort. Therefore, the whole system including the PCMHX can be assembled together on a robotic base and powered by an electric battery to achieve the movability in buildings. The air-to-refrigerant evaporator is used for providing personal cooling in the VCC-based system. A more comprehensive system experimental investigation could be found in [5]. PCMHX was designed with multiple parallel tubes with the refrigerant flowing inside tubes and PCM was filled in the annular space between PCM container and tubes as illustrated in Fig. 1(b). R134a worked as a refrigerant flowing vertically downward. Paraffin/graphite was selected as the PCM composite, in which paraffin was immersed inside the compressed, expanded natural graphite (CENG) matrix. A refrigerant distribution header and collection header were installed at the top and bottom of PCMHX, respectively, in which the refrigerant was assumed to be uniformly distributed to eight copper branch tubes. PCMHX specifications are listed in Table 1.

3. PCM condenser model

A segment-by-segment condenser model was developed for the PCMHX. Assumptions of the PCMHX model used were: (1) radiation heat to the surrounding was neglected, (2) refrigerant conduction, viscous dissipation, kinetic energy, and potential energy were neglected, (3) only thermal conduction in the CENG matrix was considered, and the effective thermal conductivity was different in the axial and radial directions, (4) the specific heat of PCM was different for the solid and liquid phases, and (5) a unit of a single tube and PCM cylinder can represent the heat transfer performance of original eight-tube PCMHX design. Fig. 1(c) is the single tube unit. To keep the same mass of PCM per tube, the cross-section of the single-tube unit was 1/8 of the original cross-section. To maintain the same heat transfer area per tube, the tube length of the single unit ( $L$ ) was the same as the eight-tube design. Paraffin wax, PureTemp37, was selected as the PCM with a melting temperature of 37°C. The thermal properties of PureTemp37 are listed in Table 2.

Table 1: PCMHX design properties

Parameters	Unit	Value
PCM container diameter	mm	265
PCM composite height	mm	280
Tube length	mm	300
Tube without PCM length	mm	20
Numbers of tubes	--	8
Tube inside diameter	mm	4.8
Tube outside diameter	mm	6.4
Header length	mm	51.8
Header inside diameter	mm	7.9
Header outside diameter	mm	9.5

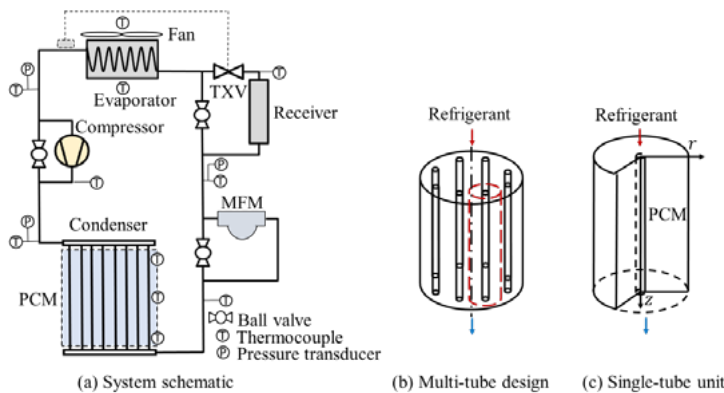


Fig. 1. PCMHX design and modeling unit (TXV: thermostatic expansion valve. MFM: mass flow meter).

Table 2. Properties of PureTemp37

Properties	Unit	Value
Melting temperature	°C	36.5–37.5
Latent heat	$\text{kJ}\cdot\text{kg}^{-1}$	210
Thermal conductivity	$\text{W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$	0.15 (liquid), 0.25 (solid)
Density	$\text{kg}\cdot\text{m}^{-3}$	840 (liquid), 920 (solid)
Specific heat	$\text{kJ}\cdot\text{kg}^{-1}\cdot\text{K}^{-1}$	2.63 (liquid), 2.21 (solid)

### 3.1. PCM side model

Under the cylindrical coordinate system, there is a rotation symmetric heat transfer to PCM with respect to the longitudinal axis (see Fig. 1(c)). Therefore, a transient two-dimensional (2D) numerical model was used to simulate heat transfer and PCM melting process in the PCM condenser. The enthalpy method was adopted for the 2-D PCM modeling. The energy equation is given by Eq. (1).  $T_p$  and  $h_p$  are PCM temperature and enthalpy, respectively.  $h_p$  is a function of PCM temperature.  $k_{p,r}$  and  $k_{p,z}$  are PCM effective thermal conductivity in radial direction and axial direction, respectively. PCM enthalpy and effective thermal conductivity are two crucial parameters that need to be determined to solve this energy equation.

$$\rho_p \frac{\partial h_p}{\partial t} = k_{p,r} \frac{1}{r} \frac{\partial}{\partial r} \left( r \frac{\partial T_p}{\partial r} \right) + k_{p,z} \frac{\partial^2 T_p}{\partial z^2} \quad (1)$$

PCM liquid fraction is given by Eq. (2) to evaluate the PCM melting process.  $T_s$  and  $T_l$  are PCM temperatures at the beginning and the end of the phase change process, respectively.

$$\lambda(T_p) = \begin{cases} 0 & h \leq h_s \\ \frac{T_p - T_s}{T_l - T_s} & h(T_s) < h < h(T_l) \\ 1 & h \geq h_l \end{cases} \quad (2)$$

The PCM effective thermal conductivity in the radial direction,  $k_{p,r}$ , and that in the axial direction,  $k_{p,z}$  are significant parameters to address this numerical problem as in Eq. (1).  $k_{p,r}$  and  $k_{p,z}$  are different due to the manufacturing process of PCM/CENG composite [7]. The thermal conductivity of the CENG matrix in the compression force direction is less than the perpendicular direction. The correlations used for effective conductivities  $k_{p,r}$  and  $k_{p,z}$  are proposed by Py et al. [8].

Boundary conditions for PCM temperature are given in Eqs. (3) to (6).  $R_i$  is the inner radius of the PCM cylinder, which is the same as the tube outer radius.  $R_o$  and  $L$  are the outer radius of the single-tube unit and the cylinder length, respectively.  $A_i$  and  $A_{top}$  is the heat transfer area contacted tube walls and the top area of the PCM cylinder, respectively.  $A_o$  is the equivalent outer heat transfer area for the single-tube unit to the surrounding.  $A_o = A_o'/8$ , in which  $A_o'$  is the outer surface area of the original multi-tube design.  $\alpha_1$ ,  $\alpha_2$  and  $\alpha_3$  are the natural convection heat transfer coefficient at the outer, top and bottom boundary, which are calculated by the correlation proposed by [9].  $T_a$  and  $T_w$  are the surrounding and wall temperatures, respectively.

$$k_{p,r} \frac{\partial T_p(r, z, t)}{\partial r} = A_i \frac{2k_w}{\delta} (T_w(z, t) - T_p(r, z, t)) \quad r = R_i \quad (3)$$

$$k_{p,r} \frac{\partial T_p(r, z, t)}{\partial r} = \alpha_1 A_o (T_p(r, z, t) - T_a) \quad r = R_o \quad (4)$$

$$k_{p,z} \frac{\partial T_p(r, z, t)}{\partial r} = \alpha_2 A_{top} (T_p(r, z, t) - T_a) \quad z = 0 \quad (5)$$

$$k_{p,z} \frac{\partial T_p(r, z, t)}{\partial r} = \alpha_3 A_{top} (T_p(r, z, t) - T_a) \quad z = L \quad (6)$$

The initial condition for PCM temperature is as follows:

$$T_p(r, z, t) = T_{ini} \quad t = 0 \quad (7)$$

A finite-volume method was adopted to solve the aforementioned governing equations for PCM. As illustrated in Fig. 2, uniform segments were applied for the discretization along with axial and radial directions in the PCM domain. Control volumes in the axial and radial directions are designated by  $i$  and  $j$ . Each PCM control volume is an annular space. The discretized energy equation for PCM heat transfer using the enthalpy method is given in Eq. (8).  $A_{p,r}$  and  $A_{p,z}$  are the heat transfer areas of each control volume in the radial direction and axial direction, respectively.

$$\begin{aligned}
 m_{p(i,j)} \frac{h_{p(i,j)}}{\partial t} = & \frac{k_{p,r}}{dr} A_{p,r(j)} (T_{p(i,j-1)} - T_{p(i,j)}) - \frac{k_{p,r}}{dr} A_{p,r(j+1)} (T_{p(i,j)} - T_{p(i,j+1)}) \\
 & + \frac{k_{p,z}}{dz} A_{p,z(j)} (T_{p(i-1,j)} - T_{p(i,j)}) - \frac{k_{p,z}}{dz} A_{p,z(j)} (T_{p(i,j)} - T_{p(i+1,j)})
 \end{aligned} \tag{8}$$

3.2. Refrigerant side model

The refrigerant flow was one-dimensional, and the conduction term was neglected. The energy equation and continuity equations of the refrigerant flow are given in Eqs. (9) and (10), respectively. Pressure ( $P$ ) and specific enthalpy ( $h$ ) were selected as state variables [10,11]. Refrigerant properties including density,  $\rho$ , the partial derivative of density with respect to enthalpy,  $(d\rho/dh)_p$ , and that with respect to pressure,  $(d\rho/dP)_h$ , were obtained by refrigerant property functions proposed in [12].

$$\frac{dU}{dt} = V \left[ \left( h \frac{d\rho}{dP} \Big|_h - 1 \right) \frac{dP}{dt} + \left( h \frac{d\rho}{dh} \Big|_p + \rho \right) \frac{dh}{dt} \right] \tag{9}$$

$$\frac{dm}{dt} = V \left( \frac{d\rho}{dP} \Big|_h \frac{dP}{dt} + \frac{d\rho}{dh} \Big|_p \frac{dh}{dt} \right) \tag{10}$$

As shown in Fig. 2, spatial discretization along the axial direction was adopted for the refrigerant flow as well. Discretized energy and continuity equations for the refrigerant are given in Eqs. (11) and (12), respectively.  $h_{in}$  and  $h_{out}$  are refrigerant enthalpy flowing into and out of the selected cross section.  $\dot{m}_{in}$  and  $\dot{m}_{out}$  are refrigerant mass flow rate flowing into and out of the selected section.  $\alpha_{ref}$  is the convective heat transfer coefficient. For single-phase flow,  $\alpha_{ref}$  is calculated from correlations proposed in [13]. For two-phase flow,  $\alpha_{ref}$  calculation was based on the correlation in [14].  $\alpha_{ref}$  of two-phase flow changes with quality  $x$ , and the smooth function was used at  $x < 0.05$  and  $x > 0.95$  to prevent discontinuities of the heat transfer coefficient at the phase transition point.

$$V_{(i)} \left( \frac{d\rho}{dP} \Big|_{h(i)} \frac{dP}{dt} + \frac{d\rho}{dh} \Big|_{p(i)} \frac{dh}{dt} \right) = \dot{m}_{(i)} - \dot{m}_{(i+1)} \tag{11}$$

$$\begin{aligned}
 V_{(i)} \left[ \left( h(i) \frac{d\rho}{dP} \Big|_{h(i)} - 1 \right) \frac{dP}{dt} + \left( h(i) \frac{d\rho}{dh} \Big|_{p(i)} + \rho_{(i)} \right) \frac{dh}{dt} \right] \\
 = \dot{m}_{(i)} h_{(i)} - \dot{m}_{(i+1)} h_{(i+1)} + \alpha_{ref(i)} A_{p,r(i)} (T_{HTF(i)} - T_w(i))
 \end{aligned} \tag{12}$$

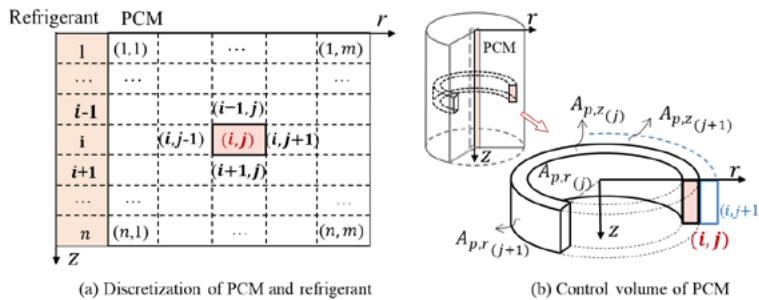


Fig. 2. Discretization of PCMHX

#### 4. Other component models

Different from most of the previous studies on water-to-PCM heat exchangers, in this paper, the refrigerant flowing inside PCM tubes is the refrigerant. Since PCM temperature profiles vary during the melting process, and affect the PCMHX performance, and thus for the VCC the refrigerant inlet states and heat transfer coefficient along the flow direction vary with time in the PCMHX. This variation can also be reflected by Eq. (3), showing that the PCM boundary condition at  $R_i$  is neither the constant heat flux nor the constant wall temperature. Therefore, to simulate the PCMHX performance, the VCC system should be modeled. Components include an evaporator, thermostatic expansion valve (TXV), compressor, receiver, and pipes.

##### 4.1. Evaporator model

A fin-and-tube heat exchanger was selected as the evaporator design. Discretized governing equations of refrigerant in evaporator are the same as those in the PCM condenser, as described in Eqs. (11) and (12). Heat transfer coefficient of refrigerant,  $\alpha_{ref}$ , was calculated using correlations propose by [15] for two-phase flow and by [13] for single-phase flow. For tube wall and fins, the energy equation is given by Eq. (13).

$$(M_w C_{p,w} + M_{fin} C_{p,fin}) \frac{dT_w}{dt} = \alpha_{ref} A_{ref} (T_w - T_{ref}) + \dot{m}_a C_{p,a} (T_{a,in} - T_{a,out}) + \dot{m}_a H_a (\omega_{a,in} - \omega_{a,out}) \quad (13)$$

In Eq. (13), the first term at the right-hand side is the heat transfer between tube walls and refrigerant, the second term means sensible heat released from air to tube walls, and the third term is the latent heat from the air.  $\dot{m}_a$ ,  $C_{p,a}$  and  $H_a$  are air mass flow rate, air specific heat, and water vaporization heat, respectively.  $T_{a,in}$ ,  $T_{a,out}$ ,  $\omega_{a,in}$  and  $\omega_{a,out}$  are air inlet temperature, outlet temperature, inlet humidity ratio and outlet humidity ratio, respectively.  $T_{a,in}$  and  $\omega_{a,in}$  are known.  $T_{a,out}$  and  $\omega_{a,out}$  can be solved by Eqs. (14) and (15), yielding air side governing equations as described by [10].

$$T_{a,out} = T_{a,in} + (T_w - T_{a,in}) \left\{ 1 - \exp \left[ - \frac{\alpha_a (A_t + \eta_{fin} A_{fin})}{\dot{m}_a C_{p,a}} \right] \right\} \quad (14)$$

$$\omega_{a,out} = \omega_{a,in} + \left\{ 1 - \exp \left[ - \frac{\alpha_a (A_t + \eta_{fin} A_{fin})}{\dot{m}_a C_{p,a} Le^{2/3}} \right] \right\} \min(0, \omega_{a,sat} - \omega_{a,in}) \quad (15)$$

$A_t$  and  $A_{fin}$  are heat transfer area of tube-side and fin-side, respectively. Fin efficiency,  $\eta_{fin}$  was calculated using correlations proposed by [16]. Airside heat transfer is enhanced by plate wavy-herringbone fins with a staggered tube layout. Thus, the air-side heat transfer coefficient,  $\alpha_a$ , was obtained from the correlations proposed by [17].  $Le$  is the Lewis number yielding  $Le^{2/3}=0.9$  [18].

##### 4.2. TXV model

The TXV model is described in [10] and [19]. TXV was assumed to be adiabatic. The expansion of the refrigerant was assumed to be isenthalpic. The refrigerant mass flow rate controlled by the TXV is given by Eq. (16), in which  $C_v$  is the flow coefficient,  $A_t$  is the flow area of the throttle,  $\Delta p$  is the pressure drop across the valve.

$$\dot{m} = C_v A_t (\rho_{in} \Delta p)^{1/2} \quad (16)$$

The refrigerant flow area was controlled by a needle movement, which reflects the superheat degree at the evaporator outlet. Valve geometry and a function to obtain the TXV bulb temperature are presented in [10]. The force balance on the diaphragm is given in Eq. (17). The sensor provides a force on the one side of the diaphragm,  $P_b A_{dia}$ , which is the same with the total forces on the other side supplied by evaporator pressure and the spring.  $k_{sp}$ ,  $y_{sp}$  and  $F_{sp,ini}$  are the spring constant, deflection and the initial force, respectively.

$$k_{sp} y_{sp} + F_{sp,ini} + P_{evap} A_{dia} = P_b A_{dia} \quad (17)$$

4.3. Compressor model

The compressor provides a refrigerant mass flow throughout the VCC. The efficiency-based compressor model was applied in this study. Volumetric efficiency,  $\eta_{vol}$ , isentropic efficiency,  $\eta_{isen}$  and motor efficiency,  $\eta_m$ , were used to calculate the compressor power consumption,  $W_{comp}$ , as given in Eqs. (18) to (20).  $\dot{m}$  and  $N$  are the mass flow rate and compressor speed, respectively.  $\rho_{in}$  is the refrigerant density at the inlet of the compressor.

$$h_{out} = h_{in} + \frac{h_{out,s} - h_{in}}{\eta_{isen}} \tag{18}$$

$$\dot{m} = \frac{\eta_{vol}\rho_{in}V_{comp}N}{60} \tag{19}$$

$$W_{comp} = \dot{m} \frac{h_{out} - h_{in}}{\eta_m} \tag{20}$$

4.4. Receiver and pipe models

The receiver model and connecting pipe model are essentially the same as the evaporator model. As described before, the refrigerant side can be solved by discretized equations as in Eqs. (11) and (12). The air-side heat transfer was based on natural convection.

5. Results

5.1. Grid sensitivity

Sensitivities to grid size and aspect ratio were investigated. The model was simulated under different grid sizes and aspect ratios as follows: 40x20, 30x10, 20x10, 10x5, and 5x5. Results are shown in Fig. 3. The deviation of both pressure and capacity between grids 40x20 and 30x10 is less than 1.0%. Therefore, the grid of 30x10 was good enough to be adopted in the simulation.

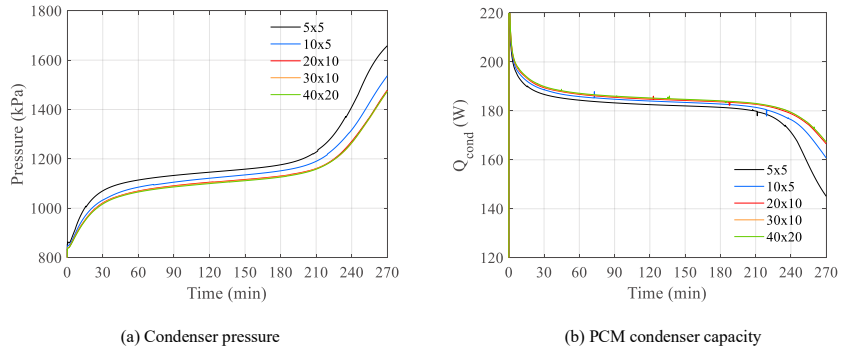


Fig. 3. Grid independence of numerical solution.

The PCMHX model and system model were developed in Dymola®. The algorithm of Lsodar was adopted, which is an implicit multi-step method. The backward differentiation formula was applied in the algorithm to solve differential equations. Time step size was determined on every step with a tolerance of  $1e^{-6}$ .

5.2. Simulation results

Fig. 4 (a)-(e) show the comparison of the experimental and numerical results on system operating pressures, condenser outlet subcooling and evaporator outlet superheat, mass flow rate, COP, and heat exchanger capacities indicating that numerical results match well with the experimental results. The good agreements illustrate that the numerical model is reliable. Fig. 4(f) shows the PCM temperatures at 1/3 from the top and bottom of the PCMHX for both numerical and experimental results. From Fig. 4(a), evaporating pressure was

almost constant due to the steady surrounding temperature. The condenser pressure increased with the cooling time due to the process of PCM melting. As the PCM absorbed heat from the condenser tube, its average temperature increased (Fig. 4(f)) and thus the condensing temperature was increased, leading to the increased of subcooling at the condenser outlet as well. Fig. 4(c) indicates mass flow rate decreased gradually, which is because the higher condensing pressure led to lower volumetric efficiency. Fig. 4(d) and (e) show the slightly decreased COP and capacity due to the increase of the condensing pressure. As can be seen from Fig. 4(f), the proposed PCMHX model can predict the PCM melting process well.

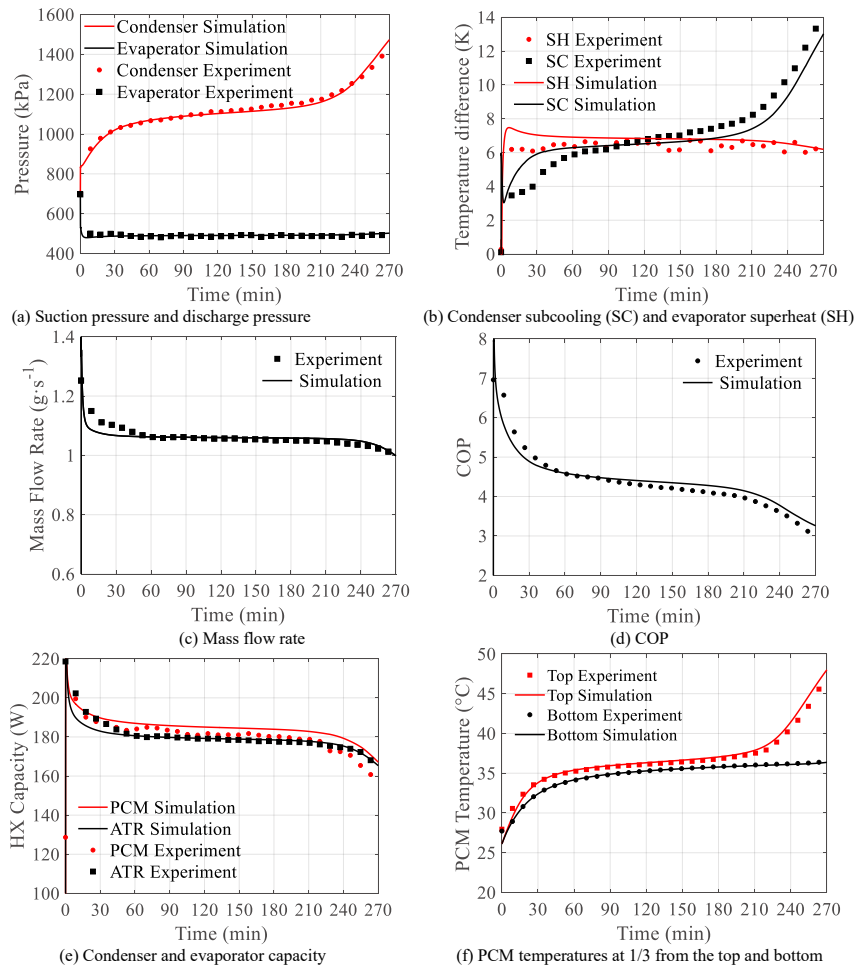


Fig. 4. Numerical results compared with experimental results.

Fig. 5 and Fig. 6 shows the numerical solution of the PCM temperature and melting fraction of the single-tube unit. The vertical direction means the condenser length direction, and the horizontal direction represents the radial direction. Refrigerant flowed downward from the top to the bottom. It can be found that the PCM melting rate decreased along the condenser length direction. The bottom PCM temperature was lower than the top and middle sections, which can also be verified by Fig. 4(f). The PCM temperature gradient in the radial direction was smaller than the axial direction. Besides, the heat transfer area of subcooled-liquid refrigerant increased with the cooling time. The refrigerant liquid zone at the bottom was greater than the vapor zone at the top near the condenser inlet. From Fig. 6, at 270 minutes, liquid fractions at the top 1/3 were higher than 0.9, while at the bottom 1/3 PCM liquid fractions were less than 0.4. This uneven PCM melting is due to the

uneven refrigerant heat transfer coefficient. At the top and middle section, the refrigerant-side heat transfer coefficient is much higher than that at the bottom because the refrigerant is in two-phase at the top and middle, while it becomes sub-cooled liquid at the bottom. It can be concluded that the utilization ratio of the PCM latent heat needs to be improved.

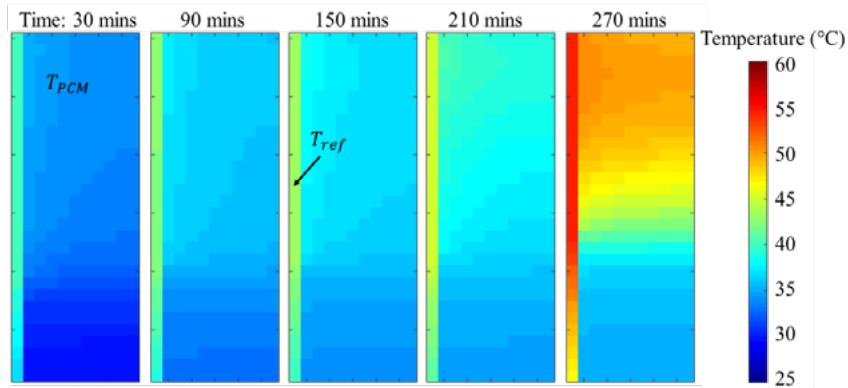


Fig. 5 PCM and refrigerant temperatures

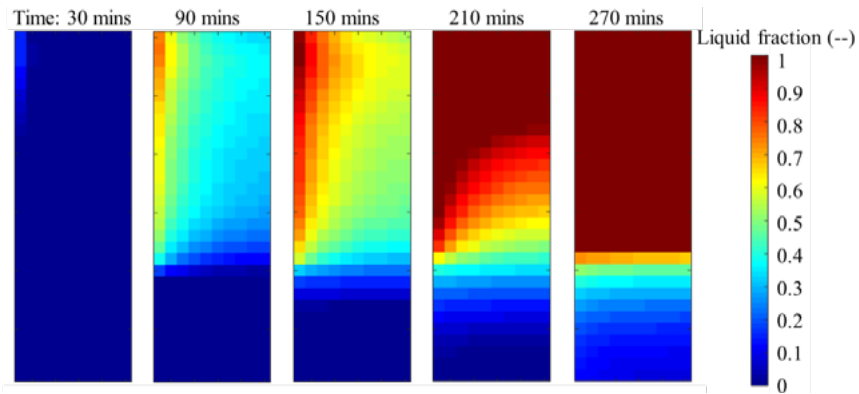


Fig. 6. PCM liquid fractions

**Conclusions**

In this paper, we developed the two-dimensional PCM-to-refrigerant heat exchanger model and transient system model of the VCC coupled with PCMHX in a personal cooling system. PCMHX works as a condenser of the VCC system and interface for thermal energy storage. Grid size sensitivity was checked, and numerical results were compared with the experimental results. It shows good agreements between simulation and experiment for both system performance and PCM heat transfer characteristics. Uneven PCM melting was also observed and reasoned due to the uneven heat transfer rate from the refrigerant to PCM along the condenser length. Therefore, a better PCMHX design should be further investigated to fully utilize the advantage of all the latent heat.

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